Geometric Analysis in Cultural Heritage

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Abstract

We present a review of recent techniques for performing geometric analysis in cultural heritage applications, targeting the broad community of researchers and practitioners in cultural heritage computing. The problems considered include shape perception enhancement, restoration and preservation support, monitoring over time, object interpretation, and collection analysis. All of these problems typically rely on an understanding of the structure of the shapes in question at both a local and global level. In this survey, we discuss the different problem forms and review the main solution methods, aided by classification criteria based on the geometric scale at which the analysis is performed and the cardinality of the relationships among object parts exploited during the analysis. We finalize the report by discussing open problems and future perspectives.

1. Introduction

Computing in Cultural Heritage (CH) has become a well-known and broad research field. Databases and text data mining for heritage applications have been lively and productive areas of computing. Among those topics, the use of computer graphics techniques in cultural heritage has been an active area of research for over the past 20 years. Advances have been made from several points of view, so that the use of graphics in cultural heritage has now grown too large to survey as a whole. While there are many ways its contributions can be categorized, one broad scheme is to consider three classes – acquisition, communication and analysis.

Many research projects have focused on the acquisition of 3D models with cultural heritage as a motivating application, going back to the 1980’s [BRTL88]. Numerous surveys have been produced for the acquisition [REH06]. Cultural heritage has some special requirements, such as limitations on touching or temporarily modifying the surface (such as by spraying with white powder), in addition to frequent financial constraints. Novel acquisition methods for cultural heritage have progressed substantially, and have proved useful for acquisition for other purposes.

Many projects have also focused on the use of graphics for illustration and public communication in cultural heritage, with surveys of these efforts already appearing more than 10 years ago [Add00]. Cultural heritage has some special requirements, such as limitations on touching or temporarily modifying the surface (such as by spraying with white powder), in addition to frequent financial constraints. Novel acquisition methods for cultural heritage have progressed substantially, and have proved useful for acquisition for other purposes.

Many projects have also focused on the use of graphics for illustration and public communication in cultural heritage, with surveys of these efforts already appearing more than 10 years ago [Add00]. These projects draw on and contribute to techniques in multimedia, human interaction and web technology. Topics such as augmented reality, mobile and gaming technologies continue being explored for presentation and public engagement.

In this STAR report, rather than considering acquisition and communication, we survey the analytical techniques that are facilitated by computer graphics after the relevant models have been acquired. In particular, we focus our attention on the vast field of analytical techniques applied to geometry that have been developed for heritage applications. These techniques are directed at experts in archaeology, history and/or conservation, rather than for communication with or engagement of the general public. Analysis is performed to answer typical questions in CH, such as “how was this made?”, “why was this object made this way?”, “who made this?”, “how has this changed through time?”, and “how can this object best be protected from damage?”. Our summary is intended for practitioners in the heritage field to know what has been accomplished, and for researchers in computer graphics to know what challenging problems remain open.

2. Related work

In this section we discuss past surveys related to computer-based techniques applied to Cultural Heritage. We draw on these surveys which in some cases treat subsets of what can be considered as analysis, and in some cases treat supersets of issues that include analysis.

Owen et al. [OBP04] present a systematic study to identify the technologies used in the cultural heritage field from

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papers presented at VAST 2003, adopting an information systems theory approach that classifies procedures into three activities: input, process or output. They also outline the trends in technologies used within cultural heritage.

Happa et al. [HMD∗10] review the current state of illuminating cultural heritage sites and objects using computer graphics. While the book edited by Stanco et al. [SBG11] covers digital imaging-driven cultural heritage preservation, Ask [Ask12] investigates and discusses possible methods of 3D documentation methodology and interpreting CH data through computer vision techniques. More broadly, Stork [Sto09] briefly summarizes how the computer vision, image analysis and computer graphics algorithms have been used to process and understand digital images of scanned art, particularly paintings and drawings.

Rather than giving a comprehensive survey of all recent computer graphics techniques used for Cultural Heritage, Scopigno et al. [SCC∗11] present some examples to show the significant impact of digital 3D models on the daily work of CH scholars, curators, and restorers, and highlight some important applications of analysis in cultural heritage, including reassembly, attribution and monitoring.

Although rather recent surveys exist on shape analysis [MWZ∗14] and shape descriptors [HPPLG11], none of them thoroughly treats the field of geometrical analysis applied to CH items. Here, we build on the insights presented by Scopigno et al. [SCC∗11], expand on the description of such techniques that have been developed for heritage, and present a broader view of the relevant literature.

3. Overview

We build the taxonomy of methods by considering the geometric scale at which the analysis is performed, the number of and the relationship between objects involved, and the CH application. The first classification consists in three groups: micro-, meso- and macro-scale analysis†. Predominantly a taxonomy of scale, we further show how approaches at micro-scale observe the geometry at the smallest possible scale, macroscopic methods consider objects as a whole, while mesoscopic techniques tend to perform an analysis of local sub-regions of the artworks. Hybrid analyses also exist, that employ operators and descriptors in a multi-scale framework. In order to classify these approaches we consider their predominant scale of analysis. For each class we explain the nature of the used 3D data, and we list the methods that study a single object, one object in relation with a set of similar samples, or that perform a many-to-many comparison. We consider also methods that perform particular geometric processing strongly related to a CH analysis. Further, we identify some general CH applications that benefit from each of them. These applications are perception enhancement, restoration and preservation, monitoring, interpretation and collection analysis. In Table 1 we show a table that summarizes our taxonomy.

Figure 1: Shape enhancement. A 3D model of Buddha statuette [Aim03]: (a) the original model lit with ambient occlusion; (b) the printed replicas of the original and geometrically enhanced models; (c) is the comparison between a small part of the original and enhanced model. In the latter, more details are better perceivable and preserved. Images courtesy of Pintus et al. [PGCS10].

4. Micro geometry

In this section we organize the literature related to the techniques that exploit small geometric features to perform analysis in the CH field. With the term micro geometry, we refer to the smallest possible portions of the surface, i.e., single or small groups of primitives. These methods use operators that, whatever is the size of the analysis kernel involved, process, extract or classify local features as primitive attributes; they represent a local measurement, and they are not intended to describe larger local sub-regions of the surface, nor an object as a whole. These innovative methodologies have been designed, implemented and assessed to follow

† Note that, compared to the definition in other fields of computer graphics such as appearance modelling, our notion of micro vs meso structure slightly differs in scale: in our taxonomy, the scale transition happens at about one order of magnitude larger scale.
### Table 1: Geometric Analysis Taxonomy.

<table>
<thead>
<tr>
<th>Scale</th>
<th>Objects</th>
<th>CH Application</th>
</tr>
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<tbody>
<tr>
<td>Micro-scale</td>
<td>Single Object</td>
<td>One-to-many</td>
</tr>
<tr>
<td></td>
<td>[CGPS08, GWS<em>09, HW11, LPC</em>00, MGW01, MKJB10, MK13, MVSL05, MMSL06, PGCS10]</td>
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<td></td>
<td>[BCP*07]</td>
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<td></td>
<td>[PTW13a, PTW13b, PSP*14, PMCS11, SSB11]</td>
<td>Perception</td>
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<td>Meso-scale</td>
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<td>[PMW*09]</td>
<td>Restoration</td>
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<td>[AIK13]</td>
<td>Monitoring</td>
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<td></td>
<td>[IT11, KS08, KS11, KPC10, SKN*12]</td>
<td>Collection Analysis</td>
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<tr>
<td>Macro-scale</td>
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<td></td>
<td>[BKMK10, LBM*13, PCMA08, RMK13]</td>
<td>Perception</td>
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<td></td>
<td>[FRB*13]</td>
<td>Monitoring</td>
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<td></td>
<td>[DCF<em>07, DST05, DB06, LCM11, MGM</em>12, DACC05]</td>
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<td>[BP10, GCJ*07]</td>
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<td>[LZZ<em>13, ZLZ</em>13]</td>
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The specific needs of real CH problems, and they are possible due to the accuracy of the 3D scanned models acquired nowadays. In the last decade, close-range 3D scanners based on laser triangulation or structured light have been developed through intensive research, both academic and industrial, and they are able to produce very dense models up to a sub-millimeter resolution.
4.1. Single object analysis

Perception enhancement. Geometric operators at fine scale are typically applied to high-resolution 3D models, to analyze and extract small structures, and enhance the details, such as impressed characters or other high-frequency signals that are difficult to perceive. These approaches typically use differential geometry coupled with multiscale frameworks. Mara et al. [MKJB10, MK13] propose a transformation invariant feature vector, that is obtained by calculating the volumes of multiple concentric spheres intersecting the volume below the 3D model’s surface at each point. They increase the readability of 3D scanned cuneiform tablets. Kolomenkin et al. [KST11] define a new direction field on surfaces (i.e., prominent field) that is oriented with respect to the prominent feature curves of the surface; they use this operator both for surface enhancement of archaeological artifacts, and for artificial coloring that can replace manual artifact illustration in archaeological reports. Levoy et al. [LPC00] use accessibility shading [Mil94] to visually enhance the appearance of chisel marks in 3D reconstructions of sculptures by Michelangelo. Polynomial Texture Map (PTM) [MGW01] and Photometric Stereo (PS) [Woo79] are other techniques that use the per-vertex computation of surface normals to increase the perception of fine geometric details in CH visualization and analysis. Hameeuw and Willems [HW11] apply PTM to increase visualization of cuneiform tablets and sealings. For instance, the acquisition and characterization of coin surface [GWS09, MVS05] overcomes visual limitations of traditional documentary techniques and provides an improved tool for numismatic understanding and coin morphology analysis. The incomplete nature of rock art drawing and photography data makes them difficult to read. Instead, PTM proved to be an efficient way to enhance the perception of petroglyphs. Mudge et al. [MMSL06] shows how the use of PTM on Paleolithic rock art allows scholars to better discern the most difficult to see surface attributes and fine details.

The enhancement of small detail perception is also very...
important in the rapid prototyping. Pintus et al. \cite{PGCS10} developed a geometry enhancement operator that counter-balances the effects due to the non-ideal behavior of the materials used in the printing process (Fig. 1). They represent the geometry as a volume, and they simulate on this volume the physical behavior of the printer. Then they compare the result to the original geometry, and modify the input data in order to reduce the difference between the original model and the printed one. Their function aims at locally increasing the contribution of geometrical high frequencies. A similar approach was presented by Cignoni et al. \cite{CGPS08}. Instead of modifying the geometry, they exploit the color painting capabilities of recent 3D printers, and propose a technique to color the surface of an object in order to enhance the perception of its geometric details (Fig. 2); they analyze the fine scale geometry to compute a counter shading signal, which is “baked” in the color attribute of each vertex before the 3D print. This approach overcomes the drawbacks of sub-surface scattering effects of the printing material, which usually blurs out the perception of the shades of the smallest details. 3D printing technology can also be used in a straightforward manner to produce replica at higher scales, or in preservation applications, such as transporting or storing CH artifacts (see section 6.1).

**Monitoring.** A general problem in CH is the measurement of preservation strategies by monitoring the micro-geometric changes over time. Many 3D acquisitions performed in a designed set of different times are useful to track fine deformation and degradation of artworks. Brunetti et al. \cite{BCP07} performed a periodic 3D scanning campaign, and showed how to measure, compare and monitor wood deformations caused by weather changes in the trees of the fossilized Dunarobba forest. They study different conservation methodologies, such as covering individual trunks with artificial roofing, maintenance of some trunks inside a climatic chamber, or surface coating of trunks by an impregnating resin product. For each area of interest they performed four 3D acquisitions with an interval of three months. They measure the modification of the area in terms of Hausdorff distance between each pair of scans, and propose the choice of the best conservation methodology with a measurable evidence.

**Interpretation.** The relief and contour lines on a group of ancient Greek red-figure vases and vase fragments are examined with the Polynomial Texture Map (PTM) \cite{MGW01}, Photometric Stereo (PS) \cite{Woot79} and 3D scanning for interpretation purposes \cite{AIK13}. They characterize the shape of lines in artworks and answer questions regarding tools, techniques, and production sequences used by Greek vase painters. They find two distinct types of relief lines, and give
4.2. Many-to-many analysis

Restoration and preservation. Micro-scale analysis and feature extraction have proven to be a central part of re-assembly applications, which address the reconstruction of fractured physical artifacts from their pieces. The pieces have generally been scattered over time, so that no a priori information is available about the whole, final, reconstructed geometry. These applications make use of various types of data – primarily geometric data, but texture and surface properties are also used. Many methods aim to be fully automatic, while others make use of user input.

While also related to computational geometry, the re-assembly of fractured objects is mostly treated as a pattern-matching problem, and respective computer vision and graphics technologies have successfully been applied for reconstructing artifacts from fragments. The main idea is to find corresponding parts, to match and align them, and to finally reassemble all matching parts. Most of the existing approaches have focused on matching and analysis of the break boundary curves of fragments as they are visually important clues for reconstruction [HFG*06, BTFN*08, YLL12].

By indexing features of the geometric information contained in the fracture surfaces of the fragments, Huang et al. [HFG*06] present a method for automatic reassembly of broken 3D solids. Yu et al. [YLL12] employ a multi-scale descriptor and conduct heat kernel-based partial matching between break boundaries, while Vendrell et al. [VVS12] use hierarchical depth maps to ensure global correction of the reconstruction and to evaluate the correspondence between fragments using an optimistic estimator. Brown et al. [BTFN*08] observe that in the case of degraded and eroded fracture surfaces, match uncertainty hampers feature-based matching; they propose a computationally efficient brute-force technique to exhaustively evaluate all possible least-squares alignments along edges of a set of fresco fragments. A recent approach [AMK14] introduces a new method for pairwise matching of broken fragments from unorganized point clouds. The new descriptor contains both a cluster of feature points and curves along the principal directions of the cluster; point cluster is obtained by analysing micro curvature of the surface, while the associated curves are approximated using Fourier series. Matching function between curves is obtained by comparing the Fourier coefficients.

Other methods employ machine learning to directly learn match likelihoods from ground-truth matches, using feature vectors describing fragment coloration, texture parameters and surface markings [TFBW*10]. Funkhouser et al. [FSTF*11] show that even when focussing on geometry alone but using a vast number of different geometric feature extractors (fig. 3), supervised learning can significantly boost the discriminative power of a pair-wise match predictor, yielding well-calibrated probabilities whether a match is correct.

Many other works, too, combine geometric and texture/color information to disambiguate reconstruction [WC08, KDSK10, ON11, ASC*13]. Kleber et al. [KDSK10], for instance, use a shape matching algorithm based on features extracted from shape, marble texture, thickness of marble fragments, and location at the excavation, to reassemble the Ephesos marble plates.

Traditionally, the documentation, administration and scientific processing of archaeological fragments are carried out manually, an intensive and time-consuming effort. Hence, some researchers turn to investigating automatic systems and semi-automatic algorithms in the hope of expediting the reconstruction process and reducing the work from the archaeologists and restoration personnel. Kampel et al. [KM03] propose two reconstruction systems, adopting the traditional archaeological methodology of using the properties of the orientation and the profile of archaeological fragments. Based on such an approach, many works have tried to make the reconstruction algorithms either semi-automatic [MRS10, BLD*12] or fully automatic [GCBR*11, YWML11, PTK01, PK03, PAE*12]. Belenguer et al. [BV12] put particular emphasis on implementation efficiency, speeding up geometric transformations, visibility tests and discretization operations by pre-calculating data and by moving all heavy calculations to the GPU.

While most reassembly approaches are bottom-up, starting from fragments, Shin et al. [SDF*12] analyzed fracture line statistics of a (manually) assembled wallpainting to study the characteristic way how frescoes break (top-down). Some of the geometric features Funkhouser et al. [FSTF*11] incorporated in their match predictor were motivated by Shin et al.’s findings. Nevertheless, such reassembly by “inverse fracture” is only in its infancy.

Some useful tools have also been developed for assisting archaeologists to analyze and reconstruct archaeological objects from their fragments [LW04b, BLD*12, PPCS12]. Fig. 4 shows the semi-automatic matching tool proposed by Brown et al. [BLD*12]. Haptics can improve an assembly task by giving feedback when objects collide [RRC*10]; Olsson et al. [ONHC13] integrate a 6-degrees-of-freedom haptic capability within a fragment alignment tool for craniomaxillofacial surgery and archaeology applications.

4.3. Discussion

The majority of the works related to micro-geometric analysis focus on two main CH applications: restoration and perception enhancement. In the first case, the local features are the key to reconstructing the (unknown) global shape of the...
final object; apart from the geometrical characterization at small scales of each single fragment, there usually is no other a priori information available to solve the reassembly problem. The second case aims at improving the perception of small-scale details of the 3D model of a given artifact, which is a valuable tool to assist scholars in their research work.

In contrast, the works classified in the monitoring, interpretation and collection analysis groups use different pipelines and mathematical representations depending on the CH item involved; they require specific information that is not independent from the particular kind of object, and is typically visible at meso or macro scales. The single work we have found in the monitoring group proposes a general framework, where the differences over time are obtained using micro features, and it can be applied to a wide range of objects, regardless of their global or local behaviour.

5. Meso geometry
We classify the data involved in the analysis as meso geometry, when the technique focuses on a particular region of the entire 3D model. These approaches use geometric operators that consider an area of the surface that is larger than a single or small groups of primitives, but they yet do not globally analyze the sample as a whole. For instance, Georgiev and Lakaemper [GL11] defined what they call mid-level geometric features, i.e., large planar sub-regions of an object, which are not the smallest available primitives (micro), nor the object as a whole (macro). Another example is the class of methods to enhance 3D visualization by local surface flattening. Local flattening doesn’t work at the primitive level (micro), nor it doesn’t try to flatten the whole object at the same time due to global geometry constraints (macro).

5.1. Single object analysis
Perception enhancement. Pietroni et al. [PMCS11] present a pipeline to analyze the 2.5D information distributed over 3D geometry, using a local 2D parameterization. They show the effectiveness of their method to solve specific CH tasks, such as the study of chisel marks over the surface for tool identification. Schmidt et al. [SSB11] transform a 3D model into a 2.5D representation as well, and apply image-based processing to the depth and reflectance signal to extract lines and contours in Chinese Buddhist stone inscriptions.

In a similar vein, Pal et al. [PTW13b, PTW13a, PSP*14] present an interactive application for browsing severely damaged documents and other cultural artefacts, which contain distortions such as wrinkling, buckling, and shrinking. In contrast to the above, their goal is not only to study the 2.5D structure, but to flatten local regions of the document for better readability of the original text, which would be impossible to do for the physical items due to their fragile condition (fig. 5). Their system consists of an interactive viewer that allows a user to browse a document while dynamically flattening only the local region under inspection. A follow-up work [PSP*14] exploits the flattening for a global restoration of damaged documents (see section 6.1).

![Figure 5: Interactive browsing of damaged documents. Severely damaged documents are acquired in 3D using a Structure-from-Motion approach. A dynamic flattening is performed while the user browses the document in order to increase its readability. We show sections of the mesh rendered in local-affine mode without flattening (left) and with local-flattening mode (right). Note that the original wrinkles remain visible since the shading is baked into the texture. Images courtesy of Pal et al. [PTW13b]](image)

Restoration and preservation. In the field of document restoration, Pintus et al. [PMW*09] present a technique that uses a flatbed scanner and Photometric Stereo (PS) [Woo79] to identify and repair scratches or tears in old documents or photographs (fig. 6). They exploit normal estimation to find creases in the almost flat surface, and they apply an infilling operator to restore original pixels. Although the texture synthesis is trained with the information from the entire image (i.e., the non-damaged part), the restoration is performed locally and it is driven by the content of the image in the local neighborhood of the damaged pixel. Conversely, in section 6.1, document restoration is a global transformation (typically an undistortion) applied to the whole page.
The pottery informatics query database (PIQD) [SKN*12] is another example of quantitative analysis applied to large sets of cultural heritage items. This is an open-source online tool that enables scholars and students to test humanities-related hypotheses against ceramic data, by defining a way to build comprehensive ceramic taxonomy and their regional spatial patterning.

Itskovich et al. [IT11] used a surface partial-matching technique in a shape classification and retrieval scenario; they apply the method to Hellenistic vases, lamps and coins inside a database, given a portion of the object as a query geometry. Their algorithm is capable of matching the correct item, even if they differ in the query location within the surface and in the level of noise.

5.3. Many-to-many analysis

Restoration and preservation. Contrary to pure feature based frameworks (see section 4.2), some assembly processes incorporate a priori knowledge about the application domain. We classify them as meso-geometric analyses, because they extract local descriptors, but they are not independent on the local or global object geometry. Pottery reconstruction, for example, benefits particularly well from exploiting the fact that most pottery was created on a potter’s wheel, that is, the final assembly is expected to be radially symmetric [WC04a, WC04b, WC08]. In its most stringent form, however, this assumption may prove unstable in the presence of very small or flat fragments [KS04] and wherever there are larger imperfections in the earthenware. Cohen et al. [CLE12] hence choose less-stringent continuity criteria by matching weighted curve moments across adjacent sherd surfaces, and Kikuchi et al. [KO13] pursue a similar goal in the context of cranial reconstruction from skull fragments: they fit a parametric Bézier surface to the surface of each neurocranial fragment to predict the surface shape of adjacent fragments, thus finding matches through surface extrapolation rather than just contour matching. Similar approaches exploit skull symmetry to drive the re-assembly and completion tasks [LYW*11, WYLL11]. Other applications, such as architectural reconstruction from fractured masonry, require extracting different structural cues, such as the main orientation of architectural features. A particularly challenging case are Gothic spires, where Laugerotte et al. [LW04a] extract dominant directions in a way resilient to the presence of ornamental features. Although lost, when the overall shape of the ruined monument is roughly known, virtual anastylosis [CFB*13, TFK*09] is another application that performs local geometrical analysis for the archaeolog-
ical and architectural reconstruction of a historic site, after a careful study of the remaining original elements.

5.4. Discussion

The techniques that combine micro feature extraction with the analysis of a bigger neighborhood of each geometrical primitive are classified as meso-scale approaches. Their region of interest is small compared to the whole object, but it is not independent from the overall nature of the topology of the geometry and other systematic shape properties. Methods in the perception enhancement and restoration groups use the same pipeline as in the micro-scale based works, but they exploit the knowledge of the object topology; for instance, the possibility to locally represent the surface as a plane enables the flattening strategy, or the analysis performed on vessels benefits well from their cylindrical structure. However, compared to other techniques, the meso-scale analysis is the best choice for collection analysis applications. The extraction of features that depend on local geometry enables the studying of a database with a huge amount of object with the same topology but with a high rate of variability. The analysis at this scale produces a good classification and successful retrieval in many practical CH cases, such as pottery, vessels, lamps, and coins.

6. Macro geometry

Macro geometry based techniques analyze a 3D model as a whole, by processing and retrieving information from a global point of view. Typical 3D models are obtained with triangulation laser scanning, time-of-flight scanners or CT volumetric acquisition devices.

6.1. Single object analysis

Perception enhancement. A useful way to document archaeological finds is the representation of so-called rollouts. The analysis of rotation-symmetric objects with paintings or inscription benefits from rollouts because they give an overall view of the CH content [RMK13]. Typically they are created either by manual drawing or from photographs. Conversely, generating 2.5D rollouts from color and geometry acquisitions represents a more reliable framework, which assists the scholars in the iconographic interpretation task. Pitzalis et al. [PCMA08] apply this analysis to the “Cylinder seal of Ibni-Sharrum”, a finely engraved object; its rollout reveals in one single 2.5D bas-relief the entire structure of the fine drawings in the seal. They combine this pipeline with the detail enhancement technique proposed by Cignoni et al. [CGPS08] (see section 4.1). Bechtold et al. [BKMK10] combine the geometry and the color to produce rollouts of figurative vase painting. They use 3D geometry from a structured light scanner to drive the transformation of the vase cylindrical topology into a 2.5D surface. For study by handling replicas, one of the most important issues is the perception and readability of the details in the printed replica (see section 4.1). Laycock et al. [LBM*13] used x-ray micro-CT technology to scan one of the 19th Century Cantonese Chess pieces with a voxel resolution of less than 9 μm. They use a straightforward scaling of the entire model, by 3D printing the model at a higher scale; this enables the scholar to appreciate both the overall structure of the chess piece and the fine surface details imperceivable in the original. Further, since those objects have an intricate internal structure, they virtually dismantle each part of the piece, so that they allow scholars to study those items separately.

Restoration and preservation. Document analysis is a topic of broad scope. Here we consider techniques that use advanced representations (such as 2.5D geometry and surface normals) to virtually restore documents and analyze their content. Documents can degrade in numerous different ways as they age. Much work has been carried out on virtually correcting the geometric distortions, scratches or tears. Some of the existing methods focus on solving the problem locally (see section 5.1), while others take into account the entire page to produce more physically coherent restoration. These latter approaches correct large distortions by capturing 3D triangle meshes of the document shape and flattening them using geometry processing techniques [BS04, SYY*05, BSY*07, PSP*14]. Others correct finer geometric distortions using image-based methods [LSC08,Lan13]. Lin et al. [LLS06] present a framework to preserve 3D documents, such as fragile bound manuscript with a non-uniform surface, documents engraved on stone, or scrolls that have been entombed in volcanic ash. They use 3D technologies to acquire the surface and to produce a physically-based 3D-to-2D transformation that converts the 3D model to a 2D image, subsequently preserving and giving a restitution of its intrinsic textual information. Another non-destructive method [SL04] was presented to reveal inaccessible text buried within damaged books and scrolls. This method is based on volumetric scanning, data modeling and physically-based simulation; it recovers readable text without physically opening or damaging the fragile items. Sanko et al. [SLMR14] use X-ray microtomography to acquire a volumetric reconstruction of a scroll of parchment that, due to its state of preservation, cannot be unrolled. The X-ray imaging picks up ink concentration, allowing for 3D reconstruction of the ink distribution followed by virtual unrolling of the scroll’s content.

Extensive and global morphological study about 3D surface characterization represents another invaluable source of qualitative and quantitative information to predict the proper restoration procedures. An important example is the scientific investigation employed in the restoration of Michelangelo’s David [CCG*04], which produced guidelines for integrating 3D data analysis in cultural heritage applications. They perform physical measures as the height of the David, its surface area and the volume; they also analyze the global geometry of the statue to evaluate the exposure to falling contaminants, such as rain, mist, or dust. Finally, a study is

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performed to visualize the center of mass projection onto its base; this helps to understand how the weight of the entire statue is distributed, and which are the corresponding weakest parts that must be preserved and eventually renovated. The high-resolution 3D model of the “Pieta” [BRM’02] has been used by Wassermann et al. [WCV’03] to study the statue’s damage and subsequent repair.

Moreover, the analysis of captured 3D models and the use of rapid prototyping are crucial for conservation and CH restitution as well. Although extensively used for perception enhancement (see section 4.1), 3D printing plays an important role in the preservation field. Transporting and storing the artifacts are complex issues, involving different packaging solutions, such as double boxing, padding negative spaces and cushioning braces. A recent paper [SEG’12] proposes the use of the generative modeling language in order to analyze the 3D model of artworks and to 3D print unique 3D-fitted containers for packaging them.

Some methods cope with the virtual and physical reconstruction of missing part of a badly damaged CH items [FMOS11]. They try to perform a completion of those parts by using the information from the scans of the whole ruined sample (e.g., by exploiting symmetry of certain objects), or from other possible hypotheses of structures based on drawings, descriptions and old texts. They also analyze feasibility of potential structural configurations [LD06]. Hess et al. [HRM’09] combine 3D laser scanning and anthropological research to deliver a holistic virtual 3D reconstruction and multimedia interactive experience of a Melanesian war canoe. The combination of reverse engineering and rapid prototyping offers a tool that overcomes limitations in some completion frameworks. Completion of the skeletal material [FdCP’08] is crucial due to the fragility of the skeletal findings, which should limit the over-handling of these fossils, and the rarity of these remains, which should avoid any task that assembles together existing and reconstructed fragments. Hence, digital modeling, 3D scanning and rapid prototyping together are essential tools that can be usefully applied for reversible and non-invasive restoration processes of damaged bones, by providing a virtual and physical restitution of a whole bone and preserving the original one.

Monitoring. Geometric acquisition and measurements produce snapshots that can be used to track global conditions of an object through time, for instance to document the evolution of an archeological destructive intervention, or based on the idea that changes over time might indicate damages. Archaeological sites are problematic case studies in the monitoring field, both during their excavation and for their long-term preservation (see also section 4.1). In the former case, fast 3D acquisition techniques are required, since a complete geometrical capture of the working site is required every day, or even every few hours. Automatic dense stereo reconstruction tools and 3D scanning are particularly suitable for monitoring of excavations [DDUC’13, CDD’11, DRDSH’14, KOC’14], and, coupled with the proper interactive tool (e.g., Meshlab [RCD’12] or Hyper3d [KRF’14]), they provide a useful workflow for objective spatio-temporal analysis and documentation.

In civil engineering, recent work on the computational and mechanical analysis for evaluating the structure and stability of bridges integrates the results of close-range digital photogrammetry, CAD tools and finite elements analysis (FEM) [AADC’07, RCAS11, RSDA’13]. Close-range photogrammetry has also been used to locate structural problems in cultural heritage monuments [AHLO05]. Some techniques analyze the damage and deformation which may have occurred depending on different aspects of construction [ARPLA10, SVG09]; they can also allow engineers and architects to estimate the influence of geometric variations in the distribution of stress [ACCLA07]. Finally, De Balestrini et al. [FdBBB’13] presented a survey methodology to investigate earthquake damages of the “Camera degli Sposi” of Mantegna (Mantova, Italy). They use both time-of-flight and triangulation laser scanners to produce multiresolution...
morphological maps of deformation, that highlight the damaged parts of the building and help to understand the damage mechanisms.

The result of the diagnostic phase is a mandatory prerequisite for the evaluation of any kind of intervention or restoration in any architectural, or artistic framework. The incomplete nature of petroglyphs drawing and photography data makes them insufficient to track the effects of natural destructive processes; 3D laser scanning was found useful to record and monitor the erosion of rock art [BCDA+05].

Interpretation. An important attribution problem in CH consists in the identification of structures that are handmade within cluttered environments. Recent studies have examined the possibility of using LiDAR in archaeological investigations to map and characterize earthworks, to capture features that may be indistinguishable on the ground and to aid the planning of archaeological excavation campaigns [LCM11, DACC05]. The approach proposed by Doneus and Briese [DB06] aims at analyzing airborne laser scanning data to identify archaeological sites within forested areas. It relies on the capability of such an acquisition device of penetrating forest to a certain degree (depending on the vegetation density), and on the possibility to compute the terrain surface even in wooded areas. In this way they are able to distinguish natural and recent features, like brushwood, or piles of twigs or wood, with small features related to the presence of an archaeological site.

Recently, high interest has arisen in the 3D morphological analysis applied to interpretation of works of art. Dellepiane et al. [DCF+07] use the data from 3D scanning and image-to-3D-model mapping in order to measure the plausibility of an attribution hypothesis of a Renaissance artifact. In a metrically objective framework they compare the global shape of a digital model of a small bronze horse to a silverpoint drawing by Leonardo, which qualitatively displays a high degree of similarity, and was thought to be drawn directly looking at the bronze. Using image-to-3D-model mapping techniques, they were able to superimpose the 3D model with the Leonardo’s drawing, giving scholars a better objective cue to solve and assess the issue of that particular disputed hypothesis. Muzzupappa et al. [MGM+12] address the interpretation problem related to the “Riaci Bronzes” statues. In particular they exploit 3D scanning techniques to study the right hand of the “Bronzo A”. They provide archaeologists with some objective data about the hand shape, by measuring a series of geometrical data such as cross-sections, deformations and volumes. This approach helps to enforce the hypothesis about the object handled by the hand, which is one of the fundamental steps to understand the statue’s identity. The use of 3D modelling and rapid prototyping is employed by Docchio et al. [DST05] in order to explore and verify a new hypothesis on the origin of the “Vittoria Alata” bronze statue, by performing a set of measurements related to distances between pairs of fiduciary points suggested by archaeologists.

In addition to attribution and identification, geometric analysis is used for the investigation of the motivation for a work or its alteration. A high resolution 3D model of Michelangelo’s Florence Pieta’ [BRM+03] was used by Wasserman et al. [WCV+03] to analyze Michelangelo’s motivation for breaking apart the statue which was subsequently reassembled by another artist. By virtually removing pieces of the work that had been repaired, Wasserman et al. were able to present the piece post-damage, and observe that it is similar in form to subsequent work by Michelangelo. They claim that the Michelangelo in breaking off pieces of the statue was acting to produce another sculpture, rather than in a fit of anger.

6.2. One-to-many analysis

Restoration and preservation. Given a damaged face appearing in a 2D image (e.g., from paintings), Lanitis et al. [LS09] describe a method to perform virtual restoration. They estimate the complete 2D shape of a face using data from the non-damaged face. Then, they compare the face with other similar samples in the training set of non-damaged faces, and predict the texture of the damaged regions. They use a similar texture synthesis approach as in Pintus et al. [PMW+09] (see section 5.1), but in their restoration framework they exploit the global transformation between the 3D and the 2D domain, by mapping the restored geometry and color back onto the original image.

Monitoring. Methods that allow to compare multiple different datasets (floor plans, drawing, 3D scans) and to explore possibilities about construction and layout are employed by Fiorillo et al. [FRB+13] to monitor the historical representations of a site over time. They compare the accurate 3D model obtained from a laser scanner system with ancient manual drawings. The basic idea is to check the global dimensional accuracy and the overall formal correctness of surveys performed by three different authors in the late 18th and in the 19th centuries.

Collection analysis. 3D scanning campaigns allow for an extensive study on how to compare similar digital objects within massive 3D databases [GCC+07]. For instance, recently, hundreds of Gallo-Roman white clay figurines coming from the center of France have been digitized using 3D scanners. Bourdeu and Pitzalis [BP10] presented a method to quantify and compare the shapes of those models. After placing homologous points (landmarks) along the entire object surface, they use geometric morphometrics, and in particular the Procrustes analysis, to extract an estimation of the difference between two shapes. This framework assists the scholars in determining the provenance of the figurines based on an objective estimation of statistical shape variability.
6.3. Many-to-many analysis

Restoration and preservation. Lu et al. [LZT*11] use the analysis and quantitative comparison between different 3D digital models of statues in a many-to-many framework, in order to solve the problem of restoring the facial sculptures in the city of Bayon. After performing a rough shape recovery using all parameterized samples in the scanned data, they performed hierarchical clustering to group similar faces. Then they refined the restoration applying the shape recovery algorithm to high resolution data in each respective cluster.

Collection Analysis. Shape comparison by using digital copies draws increasing attention in modern culture heritage studies [ZLZ*13]. Recently, a technique is presented [LZZ*13] that analyzes portrait sculptures of Augustus with 3D scanned data. It proposes a framework of automatic object categorization, where distinguishing regions are simultaneously detected. In particular, they employ a fully data-driven categorization method to extract distinguishing regions with the aim of recognizing the style of forehead hair.

Hinton et al. [HHM*11] use geometric comparison to infer the temporal sequence of the production of a series of busts of Benjamin Franklin. They considered 3D scans of marble, terra cotta and plaster models. By comparing cross sections, and taking into account the nature of the types of production, they justify a particular temporal sequence for when the previously undated busts were produced.

6.4. Discussion

All CH applications benefit from an analysis at a macro level. Unlike micro or meso approaches, since global shape, preservation condition and nature of ancient artifacts have a high variability at macro scale, even in the same category, most projects deal just with a single object. Moreover, sometimes they present analyses tailored to a particular CH test case. Studies items range from small coins to buildings, and various types of 3D acquisitions are employed, including close-range laser scanning, photogrammetry, time-of-flight scanning, and computational tomography.

Few works present results where many 3D models are compared to one another. In the restoration pipeline geometrical information of a set of object is used to digitally restore damaged or missing parts. Through time, the diversity of data acquired (images, 3D, etc) are used in a one-to-many framework for monitoring purposes. As expected, data collection benefits from the acquisition, characterization and retrieval algorithms applied to sets of CH items, such as statues organized in big databases.

7. Conclusions and Future work

The distribution of the papers in table 1 highlights a strong correlation between the scale of the analysis and the number of samples involved. Since at small scales geometrical features are “more similar”, it is possible to perform comparisons between a large number of different objects, such as “very-variable-shape” fragments of the same broken work of art; thus, a lot of contributions belong to the many-to-many class. On the other hand, the bigger the size of the CH item, the more peculiar and unique is its geometry, and the majority of methods dealing with the overall shape tend to focus on the analysis of a single artifact. As a result, the meso-scale techniques equally cover all the groups. A similar correlation is visible between scale and CH applications as well.

While macro-scale covers all kind of CH applications due to the high diversity of objects, micro and meso approaches study objects at a scale where they tend to look similar, so only few particular applications benefit from this effect. The two big clusters of methods in micro and meso analyses are respectively restoration and collection analysis. Another important element in the presented literature is the distribution of works over the time. The most papers that perform geometrical analysis were published in the last five years. This is due to the fact that 3D acquisition procedures and instruments are very mature now, and they are available at relatively low cost compared with a decade ago. These capture pipelines are more faster and easier to operate, and the size, accuracy and resolution of digital models are increasing day by day. Micro and meso analyses benefit from the high accuracy and resolution of 3D models, which are acquired with a sub-millimeter precision, while macro-scale techniques exploit the capabilities of fast laser scanner and photogrammetry to easily acquire objects ranging from small items to huge archaeological sites or buildings. Moreover, computational time has been greatly reduced in the last decade due to a great improvement of the available low cost hardware and the development of efficient parallel algorithms.

Future work will focus on two branches of the presented literature, i.e., the algorithmic and computational improvement of the analysis techniques, and the design of tools helping scholars to take the highest advantages from those approaches for their own research. Perception enhancement methods will study a compressed representation of extracted surface details, in order to allow fast access; for instance, combining stylistic analysis and sketch-based outputs will allow scholars to avoid manipulating high resolution 3D models and will support fast interpretation tasks. Although geometry reassembling for restoration was studied in many different practical test cases, it remains a challenging topic with open problems. For example, it would be interesting to study different materials and causes of failure, which produce different classes of fragments in terms of the corresponding fracture pattern. Another interesting topic would be to incorporate observed statistics of fractures and matches in a machine learning framework; classifiers could learn from previously assembled pieces or objects, and they could be applied to new artifacts. The quality of 3D models for monitoring is another issue when the acquisition time is a
critical element, such as for archaeological sites during excavation activities. Possible future improvements in this field are related to the output data from Structure from Motion (SfM) algorithm in terms of geometry and color. Nowadays SfM pipelines and photo blending techniques are evolving fast to allow high resolution results comparable to models from 3D laser scanning, and it is important to investigate which of them are more suitable for CH purposes. The use of these procedures within an CH scenario poses also the problem of defining a formal guideline for archeologists; from their testing and feedback, some relevant issues must be adapted in the acquisition pipelines and in the visualization tools, such as the placement of markers, photographic campaign strategies, the processing and the integration of the data, and annotation capabilities. A similar challenge is the design of a tool to assist researchers during the interpretation task; apart from specific studies, a generally defined framework is required to validate hypotheses or to solve debates by using objective analyses based on geometric measurements. All of these are open problems that require a lot of interaction between scholars in CH and computer scientists. As long as digital libraries are increasing, the amount of hosted 3D digital models, a lot of research is possible to test and improve classification and browsing techniques for collection analysis. New databases and new mathematical representations will advance the state-of-the-art of this field, by allowing scholars to remotely perform more efficient and fast search. Finally, of course, future work may populate some of the areas of the taxonomy we have presented that are currently empty.

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